

UNIT II DIVIDE-AND-CONQUER

Divide and Conquer Methodology – Binary Search – **Merge Sort** – Quick Sort – Heap Sort – Multiplication of Large Integers – Strassen's Matrix Multiplication



Mergesort

- Split array A[0..*n*-1] into about equal halves and make copies of each half in arrays B and C
- Sort arrays B and C recursively
- Merge sorted arrays B and C into array A as follows:
 - Repeat the following until no elements remain in one of the arrays:
 - compare the first elements in the remaining unprocessed portions of the arrays
 - copy the smaller of the two into A, while incrementing the index indicating the unprocessed portion of that array
 - Once all elements in one of the arrays are processed, copy the remaining unprocessed elements from the other array into A.



Pseudocode of Mergesort

ALGORITHM Mergesort(A[0..n - 1])

//Sorts array A[0..n - 1] by recursive mergesort //Input: An array A[0..n - 1] of orderable elements //Output: Array A[0..n - 1] sorted in nondecreasing order **if** n > 1

copy A[0..[n/2] - 1] to B[0..[n/2] - 1]copy A[[n/2]..n - 1] to C[0..[n/2] - 1]*Mergesort*(B[0..[n/2] - 1]) *Mergesort*(C[0..[n/2] - 1]) *Merge*(B, C, A)



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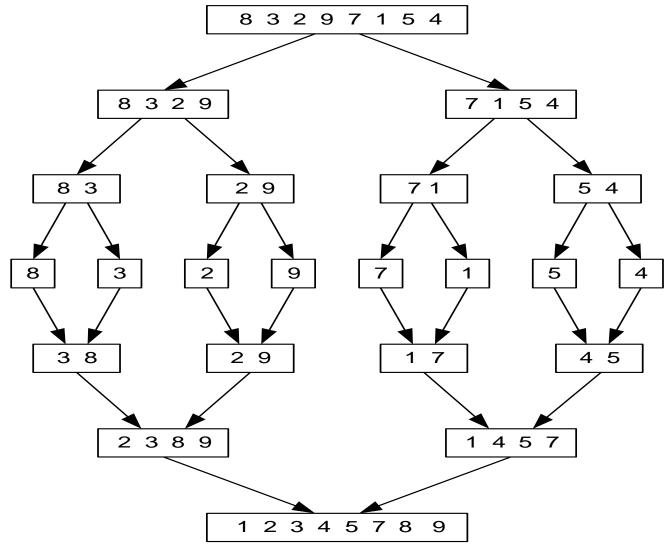
Pseudocode of Merge

Merge(B[0...p-1], C[0..q-1], A[0...p+q-1])ALGORITHM //Merges two sorted arrays into one sorted array //Input: Arrays B[0..p-1] and C[0..q-1] both sorted //Output: Sorted array A[0..p+q-1] of the elements of B and C $i \leftarrow 0; i \leftarrow 0; k \leftarrow 0$ while i < p and j < q do if $B[i] \leq C[j]$ $A[k] \leftarrow B[i]; i \leftarrow i+1$ else $A[k] \leftarrow C[j]; j \leftarrow j+1$ $k \leftarrow k+1$ if i = pcopy C[i...q-1] to A[k...p+q-1]else copy B[i..p-1] to A[k..p+q-1]Time complexity: $\Theta(p+q) = \Theta(n)$ comparisons

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Mergesort Example



The non-recursive version of Mergesort starts from merging single elements into sorted pairs.

Name of the Faculty: Dr. Sasikumar Periyannan

GALGOTIAS UNIVERSITY

Program Name: B.Sc., (Hons) Computer Science



Analysis of Mergesort

- All cases have same efficiency: $\Theta(n \log n)$ $T(n) = 2T(n/2) + \Theta(n), T(1) = 0$
- Space requirement: $\Theta(n)$ (<u>not</u> in-place)
- Can be implemented without recursion (bottom-up)

