

School of University Polytechnic
Diploma in Civil Engineering
Summer Term Examination – July - August 2024

Duration : 180 Minutes
Max Marks : 100

Sem II - N1DF201T- MATD1011 - Applied Mathematics II

General Instructions
Answer to the specific question asked
Draw neat, labelled diagrams wherever necessary
Approved data hand books are allowed subject to verification by the Invigilator

- 1) Find the derivative $\log \sin x$ with respect to x . K1 (2)
- 2) Show that $\left(\frac{-1+i\sqrt{3}}{2}\right)^3 = 1$ K2 (4)
- 3) Show that $f(\theta) = \sin\theta$, is increasing in the interval $\left(0, \frac{\pi}{2}\right)$ K2 (6)
- 4) Identify $\frac{dy}{dx}$, when: $y = (\sin^{-1} x)^x$. K3 (9)
- 5) If $a = \cos \alpha + i \sin \alpha$, $b = \cos \beta + i \sin \beta$ and $c = \cos \gamma + i \sin \gamma$ find the value of $\frac{abc}{c}$. K3 (9)
- 6) Evaluate If $x + \frac{1}{x} = 2\cos\theta$, Prove that $x^n + \frac{1}{x^n} = 2\cos n\theta$. K5 (10)
- 7) Simplify: $\int_0^1 \sin^{-1}\left(\frac{2x}{1+x^2}\right) dx$ K4 (12)
- 8) Evaluate If $\log y = \tan^{-1} x$, prove that $(1 + x^2) y_2 + (2x - 1) y_1 = 0$ K5 (15)
- 9) Evaluate $z^7 + 1 = 0$, z is a complex number. K5 (15)
- 10) Solve the If $y = e^{m \sin^{-1} x}$, then show that $(1 - x^2) \frac{d^2 y}{dx^2} - x \frac{dy}{dx} - m^2 y = 0$ K6 (18)