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| ADMISSION NUMBER |  |  |  |  |  |  |  |  |  |  |  |
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**School of Basic Sciences**  
**Bachelor of Science Honours in Physics**  
**Mid Term Examination - Nov 2023**

**Duration : 90 Minutes**  
**Max Marks : 50**

**Sem III - C1UD302T - Mathematical Physics II**

General Instructions

*Answer to the specific question asked*

*Draw neat, labelled diagrams wherever necessary*

*Approved data hand books are allowed subject to verification by the Invigilator*

- 1) State the condition for Fourier series to be integrated term wise. K2 (2)
- 2) Identify whether the function is even or odd, (i)  $f(x) = \sin 3x$  (ii)  $f(x) = x \cos x$ , and (iii)  $f(x) = x^3 - 4x$  K1 (3)
- 3) Obtain a Fourier series of function given as  $f(x) = 3 - 2x$ ,  $-\pi < x < \pi$  K2 (4)
- 4) Expand the given function in cosine series  $f(x) = e^{-x}$ ,  $0 < x < 1$  K2 (6)
- 5) Explain the importance of Fourier Series in signal systems K3 (6)
- 6) Analyze the Fourier series representing the function as, K3 (9)  

$$f(x) = \begin{cases} 0, & -\pi < x < 0 \\ 1, & 0 \leq x < \pi \end{cases}$$
- 7) Obtain the complex form of Fourier series of function,  $f(x) = x^2$  in the interval  $[-1, 1]$ . K4 (8)
- 8) Find Fourier series of a function  $f(x) = \begin{cases} 0, & -\pi < x < 0 \\ \sin x, & 0 \leq x < \pi \end{cases}$  hence prove that K4 (12)  

$$\frac{\pi}{4} = \frac{1}{2} + \frac{1}{1.3} - \frac{1}{3.5} + \frac{1}{5.7} - \frac{1}{7.9} + \dots$$

**OR**

Obtain complex form of Fourier series for the given function  $f(x) = e^{(-x)}$ , in the interval  $-\pi < x < \pi$  K4 (12)