

School of Basic Sciences
Bachelor of Science Honours in Mathematics
Mid Term Examination - Nov 2023

Duration : 90 Minutes
Max Marks : 50

Sem I - C1UC103T - Trigonometry and Analytical Geometry

General Instructions

Answer to the specific question asked

Draw neat, labelled diagrams wherever necessary

Approved data hand books are allowed subject to verification by the Invigilator

- 1) Find the sum of nth roots of unity. K2 (2)
- 2) Classify the nature of conic section $ax^2 + 2hxy + by^2 + 2gx + 2fy + c = 0$ K1 (3)
- 3) Show That $e^{2\theta} = n\pi + \frac{\pi}{2} + \alpha$ *if* $\tan(\theta + i\phi) = \tan \alpha + i \sec \alpha$ K2 (4)
- 4) Show that $\cot^{-1} \frac{3-2i}{3+2i} = \frac{\pi}{4} + \frac{i}{2} \log 5$ K2 (6)
- 5) Simplify $\frac{1+7i}{(2-i)^2}$ in the modulus-amplitude form K3 (6)
- 6) Express $\frac{1-i}{1+i}$ in the modulus-amplitude form K3 (9)
- 7) *if* $\sin \alpha + \sin \beta + \sin \gamma = \cos \alpha + \cos \beta + \cos \gamma = 0$ K4 (8)
 $\sin 3\alpha + \sin 3\beta + \sin 3\gamma = 3 \sin(\alpha + \beta + \gamma)$ show that
- 8) Formulate the polar equation of a conic the focus being the pole . K4 (12)

OR

Find the equation to the plane through (α, β, γ) , parallel to the plane $ax+by+cz=0$ K4 (12)