

# School of Basic Sciences

Department of Basic Sciences

Mid Term Examination

Exam Date: 30 Sep 2023

Time : 90 Minutes

Marks : 50

## Sem V - C1UC503T - Number Theory and Game Theory

*Your answer should be specific to the question asked*

*Draw neat labeled diagrams wherever necessary*

- 1) Estimate  $\phi(1105)$ , where  $\phi$  is Euler-phi function. K2 (2)
- 2) Find the number of positive integers  $\leq 3076$  and not divisible by 24. K1 (3)
- 3) Show if 1601 is a prime number K2 (4)
- 4) Explain that  $f(x) = 1/(1-x)^2$  is the generating function for 1, 2, 3, 4, . . . . K2 (6)
- 5) Applying Wilson's theorem, find is the remainder when 100! is divided by  $97^2$  K3 (6)
- 6) Develop a generating function for each of the following sequences K3 (9)  
(a) 2, 4, 6, 8, 10, . . . .  
(b) 1, 5, 25, 125, . . . .
- 7) For two integers 540 and 168, examine the gcd (greatest common divisor) of both and write gcd as linear combination of these two integers using Euclidean algorithm. K4 (8)
- 8) Analyse and solve the recurrence relation  $a_n = 3a_{n-1} - 2a_{n-2}$  with initial conditions  $a_0 = 1$  and  $a_1 = 3$  K4 (12)

**OR**

Consider the recurrence relation 3,6,12,24,48..... Analyse it in terms of initial condition, solution and general solution. K4 (12)